



Stathern  
Primary  
School

*'Nurture, Inspire, Discover, Create'*

## Calculation Policy

2023-2025

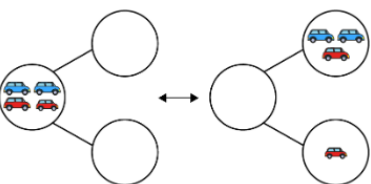

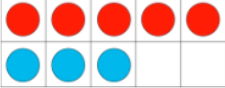

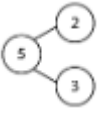

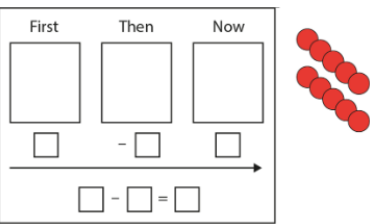

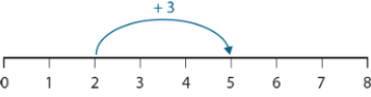

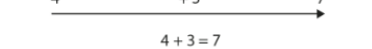
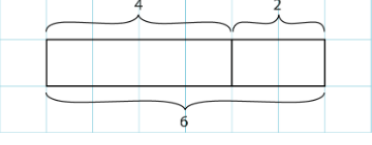
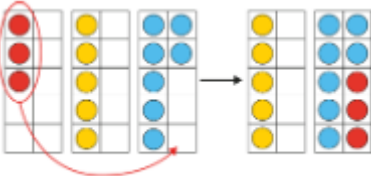
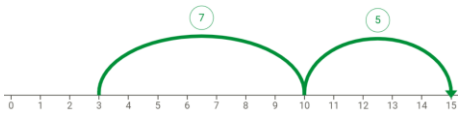
Reviewed by the Head teacher, Maths Subject Lead, teaching staff and the Maths Link Governor:

Signed: 



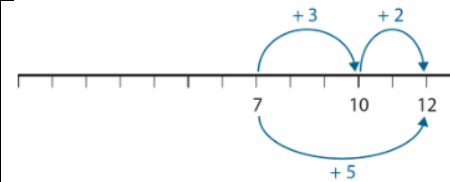
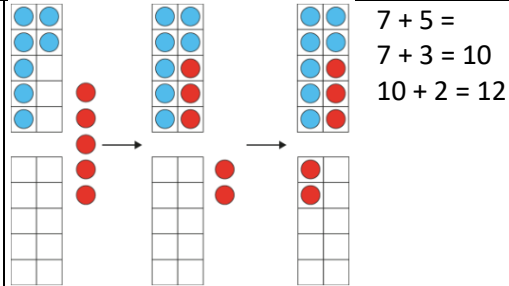
Our planning at Stathern is informed by the national curriculum, the DFE's non-statutory Ready to Progress guidance and the NCETM's prioritisation and professional development materials. This policy has been written using these documents to exemplify each of the 4 strands of calculation and summarise how this is to be taught through sentence stems, concrete, pictorial and abstract levels of understanding. Year groups have been added alongside as a guide. Ongoing assessment of pupils understanding informs our teaching. The steps in learning, challenges and approaches should always be adapted as necessary and based on pupils' security of understanding and readiness to progress to the next stage. At all stages of their learning children are encouraged to think deeply about the mathematical concepts introduced to them, apply these in a variety of ways and reflect on ways to be efficient and flexible in their calculation choices.

# Addition

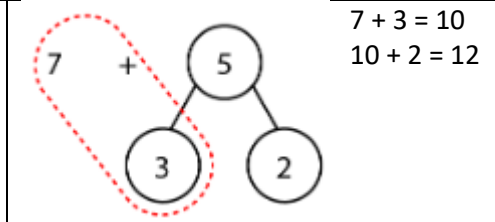
Stem sentences	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)
<p>__ is the whole, __ is a part, __ is a part.</p> <p>__ = __ plus __ and __ plus __ = __</p> <p>There are __ in total.</p> <p><b>Year 1</b></p>	  $3 + 4 = 7$ $7 = 3 + 4$ $4 + 3 = 7$ $7 = 4 + 3$  $5 + 3 = 8$ $8 = 5 + 3$ $3 + 5 = 8$ $8 = 3 + 5$	 $3 + 2 = 5$ $2 + 3 = 5$ $5 = 3 + 2$ $5 = 2 + 3$	 $2 + 3 = 5$ $3 + 2 = 5$ $5 = 2 + 3$ $5 = 3 + 2$ <p>Bar model</p> 
<p>First... Then... Now...</p> <p>e.g. <b>First</b> there were 4 children on the bus, <b>then</b> 3 children got on. <b>Now</b> there are 7 children on the bus.</p> <p><b>Year 1</b></p>	<p>Role play getting 'on the bus' or use a toy bus.</p> 	<p>First   Then   Now   <math>4 + 3 = 7</math></p>   $2 + 3 = 5$	<p>First   Then   Now</p>   $4 + 3 = 7$  $4 + 2 = 6$
<p>We can look for pairs of addends which sum to 10.</p> <p>__ plus __ is equal to 10, then 10 plus __ is equal to __.</p> <p><b>Year 2</b></p>	 $3 + 5 + 7 = 5 + 10$	<p>Pictorial representations of the tens frames OR</p> 	$3 + 5 + 7 = 3 + 7 + 5 = 10 + 5 = 15$

First I partition the \_\_: \_\_ plus \_\_ is equal to \_\_.  
 Then \_\_ plus \_\_ is equal to ten ...  
 and ten plus \_\_ is equal to \_\_.

Year 2

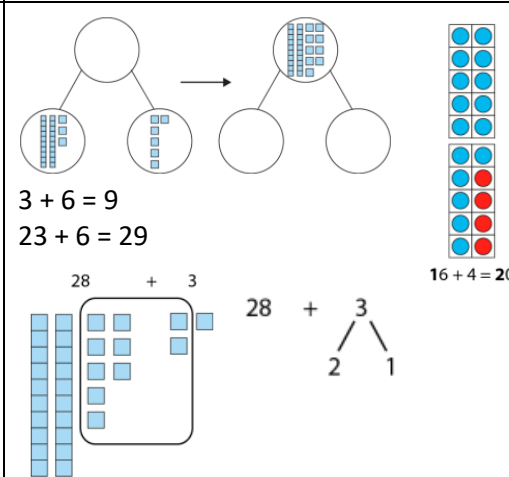


$7 + 5 =$   
 $7 + 3 = 10$   
 $10 + 2 = 12$

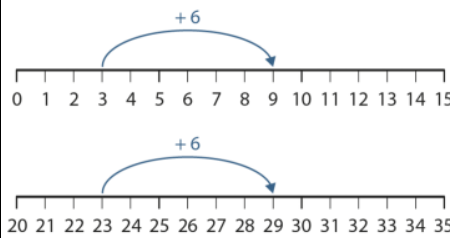


I know that \_\_ plus \_\_ is equal to \_\_. (single-digit fact)  
 So \_\_ plus \_\_ is equal to \_\_. (related two-digit plus single digit fact)  
 I know that \_\_ plus \_\_ is equal to ten so \_\_ plus \_\_ is equal to \_\_.

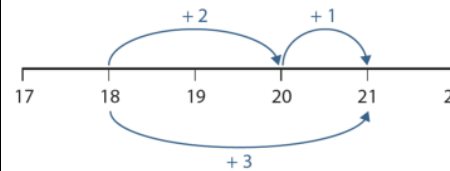
Year 2



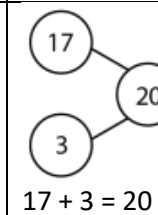
Pictorial representations of the equipment used OR



$3 + 6 = 9$



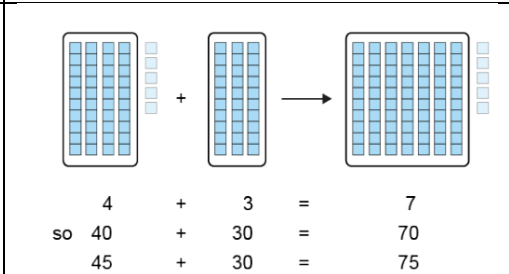
$23 + 6 = 29$



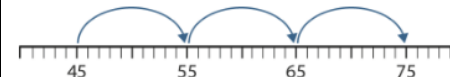
$17 + 3 = 20$

I know that \_\_ plus \_\_ is equal to \_\_.  
 So \_\_ tens plus \_\_ tens is equal to \_\_ tens.  
 \_\_ tens and \_\_ ones, plus \_\_ tens is equal to \_\_ tens and \_\_ ones.

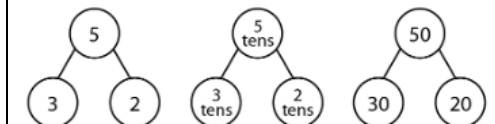
Year 2



Pictorial representations of the equipment used OR

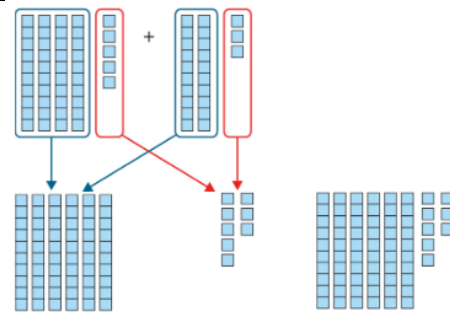


$45 + 30 = 75$



$2 + 3 = 5$   
 $2 \text{ tens} + 3 \text{ tens} = 5 \text{ tens}$   
 $20 + 30 = 50$

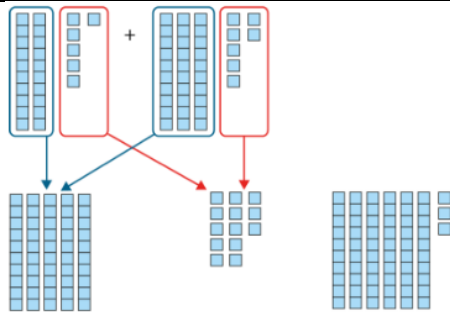
First I partition the    into    and   , and the    into    and   .  
   plus    is equal to   ... (addition of the tens)  
   plus    is equal to   ... (addition of the ones)  
and    plus    is equal to   . (addition of the tens and ones)  
So    plus    is equal to   . (summary of the overall calculation)



$$45 + 23 = 60 + 8 = 68$$

**Year 2**

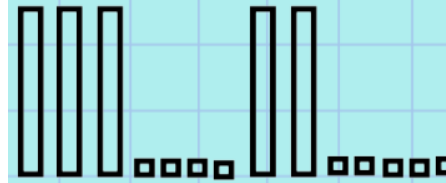
First I partition the    into    and   , and the    into    and   .  
   plus    is equal to   ... (addition of the tens)  
   plus    is equal to   ... (addition of the ones)  
and    plus    is equal to   . (addition of the tens and ones)  
So    plus    is equal to   . (summary of the overall calculation)



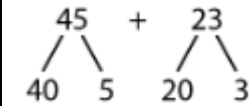
$$26 + 37 = 50 + 13 = 63$$

**Year 2**

*Real story*



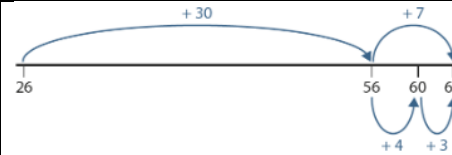
$$34 + 25 =$$



$$40 + 20 = 60$$

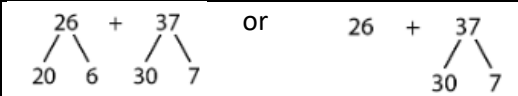
$$5 + 3 = 8$$

$$60 + 8 = 68$$



$$26 + 30 = 56$$

$$56 + 7 = 63$$



$$20 + 30 = 50$$

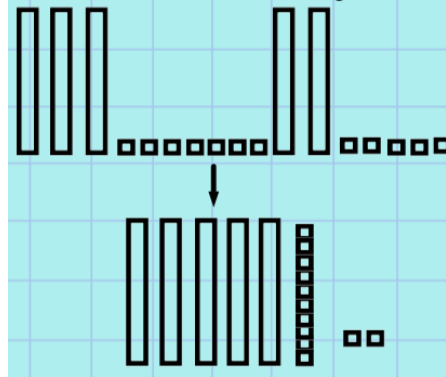
$$6 + 7 = 13$$

$$50 + 13 = 63$$

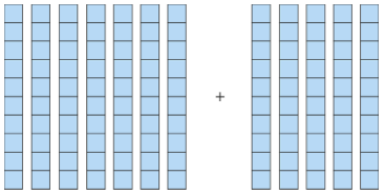
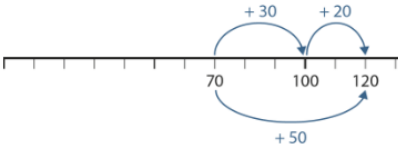
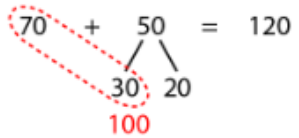
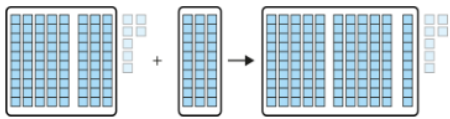
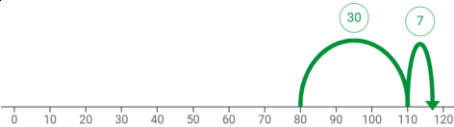
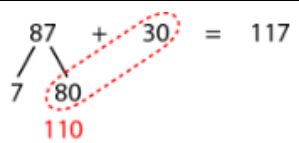
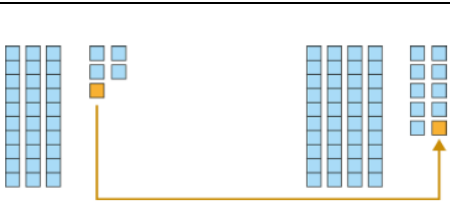
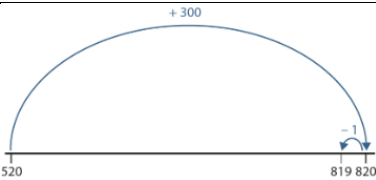
$$26 + 30 = 56$$

$$56 + 7 = 63$$

*Real story*



$$37 + 25 = 62$$

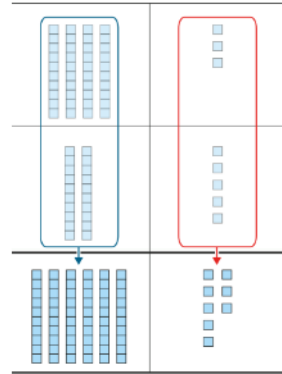
Stem sentences	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)
<p>I know that <u>  </u> plus <u>  </u> is equal to <u>  </u>. (single-digit addends)            So <u>  </u> tens plus <u>  </u> tens is equal to <u>  </u> tens. (multiple-of-ten addends)  <u>  </u> plus <u>  </u> is equal to one hundred and <u>  </u>.</p> <p><b>Year 3: Adding Multiples of 10 using scaled facts</b></p>	 <p>7 + 5 = 12            7 tens + 5 tens = 12 tens            70 + 50 = 120</p> <p>OR place value counters</p>	<p>Could include pictorial representations of equipment or:</p>  <p>70 + 50 =            70 + 30 = 100            100 + 20 = 120</p>	 <p>70 + 50 = 70 + 30 + 20            = 100 + 20            = 120</p>
<p>I know that <u>  </u> plus <u>  </u> is equal to <u>  </u>. (single-digit addends)            So <u>  </u> tens plus <u>  </u> tens is equal to <u>  </u> tens. (multiple-of-ten addends)  <u>  </u> plus <u>  </u> is equal to one hundred and <u>  </u>.</p> <p><b>Year 3: Adding 2 digit numbers mentally</b></p>	 <p>87 + 30 = 110 + 7 = 117</p> <p>OR place value counters</p>	 <p>87 + 30 = 80 + 30 + 7            = 110 + 7            = 117</p>	 <p>87 + 30 = 80 + 7 + 30            = 110 + 7            = 117</p>
<p>First we add: <u>  </u> plus <u>  </u> is equal to <u>  </u> ...            ... then we adjust: <u>  </u> minus <u>  </u> is equal to <u>  </u>.</p> <p><b>Year 3: Adding through adjusting</b></p>	 <p>35 +            49 =            34 +            50 =            84</p>	 <p>520 + 299 =            520 + 300 = 820            820 - 1 = 819</p>	<p>69 + 69 = 138</p> <p>70 + 70 = 140</p> <p>← -2</p>

**Year 3: Written methods: Adding 2 or 3 digit numbers through column methods**

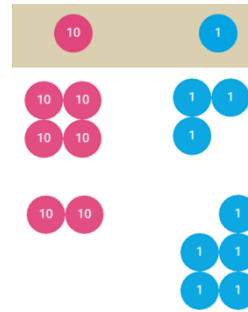
We line up the ones; \_\_\_ ones plus \_\_\_ ones.  
 We line up the tens; \_\_\_ tens plus \_\_\_ tens.  
 The \_\_\_ is in the ones column – it represents \_\_\_ ones. The \_\_\_ is in the ones column – it represents \_\_\_ ones.  
 \_\_\_ ones plus \_\_\_ ones is equal to \_\_\_ ones.  
 The \_\_\_ is in the tens column – it represents \_\_\_ tens. The \_\_\_ is in the tens column – it represents \_\_\_ tens.  
 \_\_\_ tens plus \_\_\_ tens is equal to \_\_\_ tens.

In column addition we start at the right-hand side.

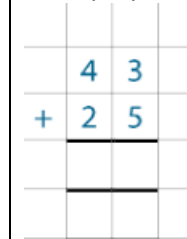
Start with two-digit numbers to exemplify lining up the columns.



Children could draw place value counters.



Start with two-digit numbers to exemplify lining up the columns.

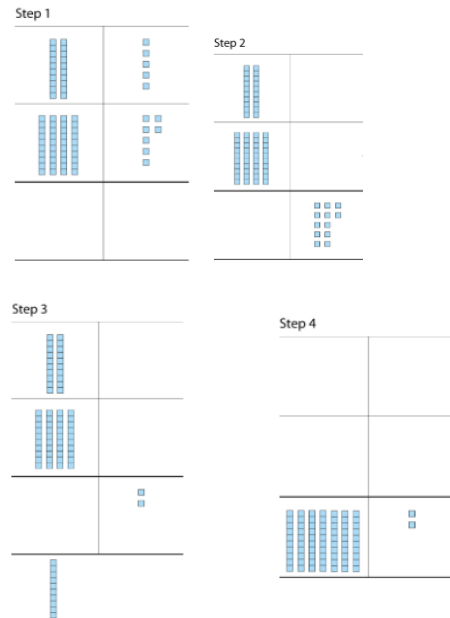


$$\begin{array}{r} 462 \\ + 205 \\ \hline \end{array}$$

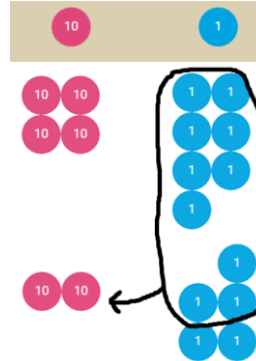
If the column sum is equal to ten or more, we must regroup.  
 \_\_\_ ones is the same as \_\_\_ ten

**Year 3: As above with regrouping**

Start with two-digit numbers to exemplify the regrouping.



Children could draw place value counters.



Start with two-digit numbers to exemplify the regrouping.

$$\begin{array}{r} 25 \\ + 47 \\ \hline 72 \\ 1 \end{array} \qquad \begin{array}{r} 25 \\ + 47 \\ \hline 72 \\ 1 \end{array}$$

$$\begin{array}{r} 567 \\ + 233 \\ \hline 800 \\ 11 \end{array}$$

If the column sum is equal to ten or more, we must regroup.

**Year 4, 5 and 6**

See Year 3 examples

See Year 3 examples

As in Year 4 but using numbers with more than 4 digits

$$\begin{array}{r} 6,584 \\ + 2,739 \\ \hline 9,323 \\ 1\ 1\ 1 \\ \hline \pounds 24.55 \\ + \pounds 17.82 \\ \hline \pounds 42.37 \\ 1\ 1 \end{array}$$

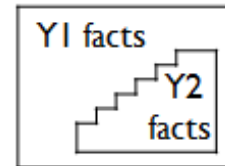
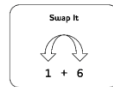
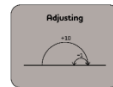
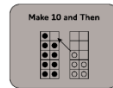
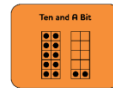
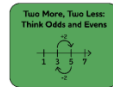


# Addition – Known Number Facts

KS1

## Addition Grid Facts

+	0	1	2	3	4	5	6	7	8	9	10
0	0+0	0+1	0+2	0+3	0+4	0+5	0+6	0+7	0+8	0+9	0+10
1	1+0	1+1	1+2	1+3	1+4	1+5	1+6	1+7	1+8	1+9	1+10
2	2+0	2+1	2+2	2+3	2+4	2+5	2+6	2+7	2+8	2+9	2+10
3	3+0	3+1	3+2	3+3	3+4	3+5	3+6	3+7	3+8	3+9	3+10
4	4+0	4+1	4+2	4+3	4+4	4+5	4+6	4+7	4+8	4+9	4+10
5	5+0	5+1	5+2	5+3	5+4	5+5	5+6	5+7	5+8	5+9	5+10
6	6+0	6+1	6+2	6+3	6+4	6+5	6+6	6+7	6+8	6+9	6+10
7	7+0	7+1	7+2	7+3	7+4	7+5	7+6	7+7	7+8	7+9	7+10
8	8+0	8+1	8+2	8+3	8+4	8+5	8+6	8+7	8+8	8+9	8+10
9	9+0	9+1	9+2	9+3	9+4	9+5	9+6	9+7	9+8	9+9	9+10
10	10+0	10+1	10+2	10+3	10+4	10+5	10+6	10+7	10+8	10+9	10+10



KS2

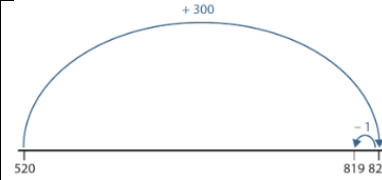
Strategy	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)
Bridging through a multiple of 10, 100, etc  <b>Years 3, 4, 5 and 6</b>	<p>7 + 5 = 7 + 3 = 10 10 + 2 = 12</p>	<p>7 + 5 = 7 + 3 = 10 10 + 2 = 12</p>	<p>7 + 3 = 10 10 + 2 = 12</p>

Compensating – rounding to the nearest multiple 10, 100, etc and adjusting

**Years 3, 4, 5 and 6**



$$35 + 49 = 34 + 50 = 84$$



$$\begin{aligned} 520 + 299 &= \\ 520 + 300 &= 820 \\ 820 - 1 &= 819 \end{aligned}$$

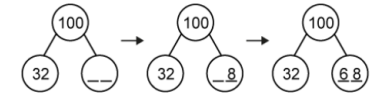
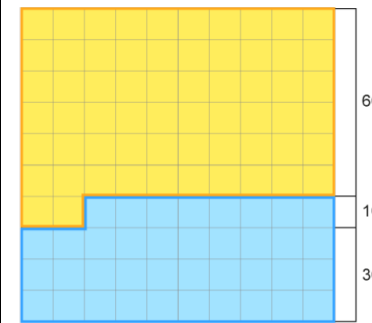
$$\begin{aligned} 69 + 69 &= \boxed{138} \\ 70 + 70 &= \boxed{140} \end{aligned}$$

← -2

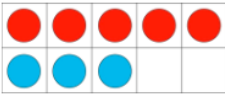
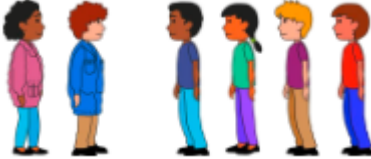

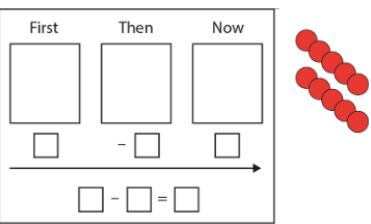
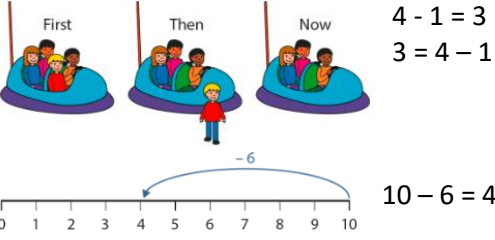
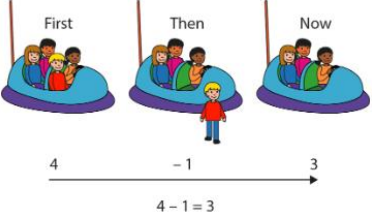
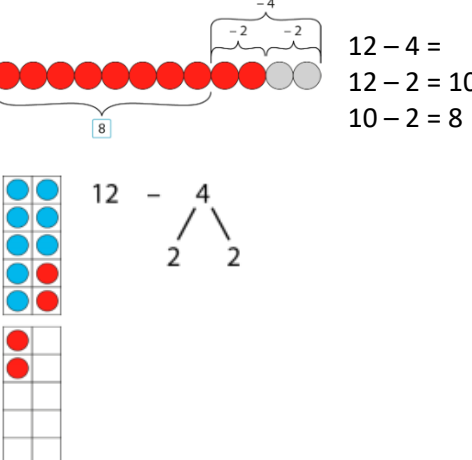
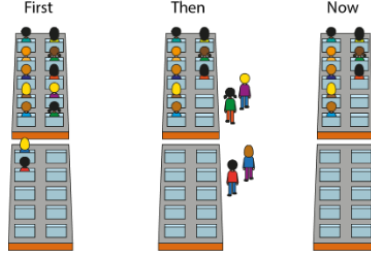
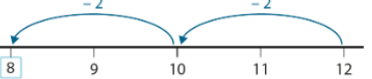
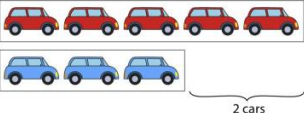
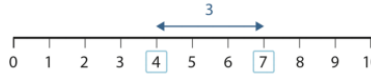
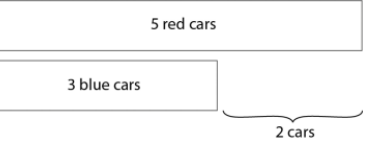
**Year 3**  
Derive quickly: Compliments to 100

First we make 10 ones. The ones digits add up to 1 ten, so we need 9 more tens.

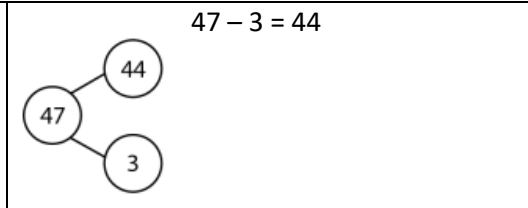
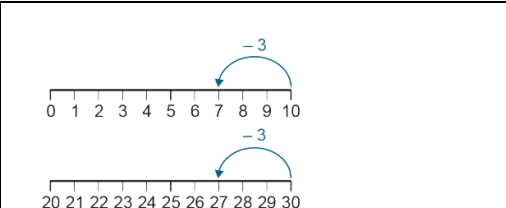
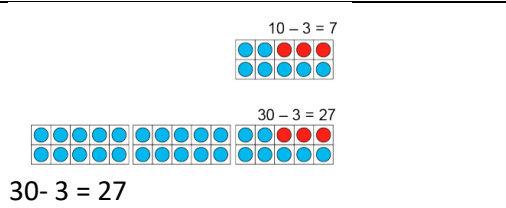
Working using Dienes or place value counters, adding ones then tens.



## Subtraction

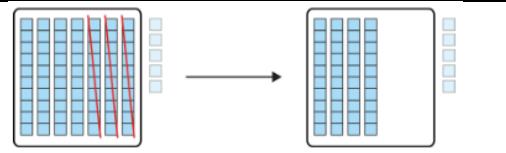
Stem sentences	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)
<p>___ is the whole, ___ is a part, ___ is a part.</p> <p>___ = ___ minus ___ and ___ minus ___ = ___</p> <p><b>Year 1</b></p>	<p>I have 8 counters. 5 counters are red. How many are blue?</p> 	<p>There are 6 children. 2 have their coat on. How many do not have their coat on?</p> 	<p>There are 8 flowers. 2 are red and the rest are yellow. How many are yellow?</p>  <p><math>8 - 2 = 6</math></p>
<p>First... Then... Now...</p> <p>e.g. <b>First</b> there were 4 children in the car, <b>then</b> 1 child got out. <b>Now</b> there are 3 children in the car.</p> <p><b>Year 1</b></p>	<p>Role play 'getting out of a car'.</p> 	 <p><math>4 - 1 = 3</math> <math>3 = 4 - 1</math></p> <p><math>10 - 6 = 4</math></p>	 <p><math>4 - 1 = 3</math></p>
<p>We partition the ___ into ___ and ___.</p> <p>First we subtract the ___ from ___ to get to 10.</p> <p>Then we subtract the remaining ___ from 10.</p> <p>We know 10 minus ___ is equal to ___.</p> <p><b>Year 2</b></p>	 <p><math>12 - 4 =</math> <math>12 - 2 = 10</math> <math>10 - 2 = 8</math></p>	<p>First there were 12 children on the ride. Then 4 got off. Now there are 8 children on the ride.</p> 	 <p><math>12 - 4 =</math> <math>12 - 2 = 10</math> <math>10 - 2 = 4</math></p>
<p>There are more ___ than ___.</p> <p>There are fewer ___ than ___.</p> <p>The difference between ___ and ___ is ___.</p> <p><b>Year 2</b></p>	 <p>The difference between 2 and 5 is 3. The difference between 5 and 2 is 3.</p>	 <p>The difference between 4 and 7 is 3. The difference between 7 and 4 is 3.</p>	 <p><math>5 - 3 = 2</math></p>

I know that    minus    is equal to   .  
 (single-digit fact)  
 So    minus    is equal to   . (related two-digit minus single digit fact)  
 I know that ten minus    is equal to    so    minus    is equal to   .

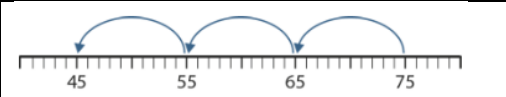


**Year 2**

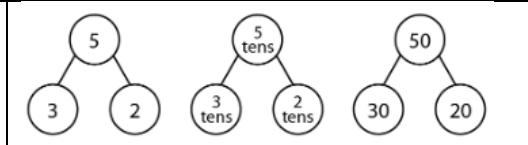
I know that    minus    is equal to   .  
 So    tens minus    tens is equal to    tens.



70 - 30 = 40 so 75 - 30 = 45

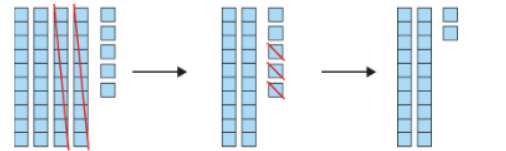


75 - 30 = 45



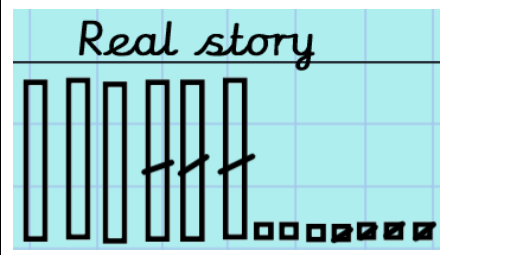
5 - 3 = 2  
 5 tens - 3 tens = 2 tens  
 50 - 30 = 20

First I subtract the tens, then I subtract the ones.



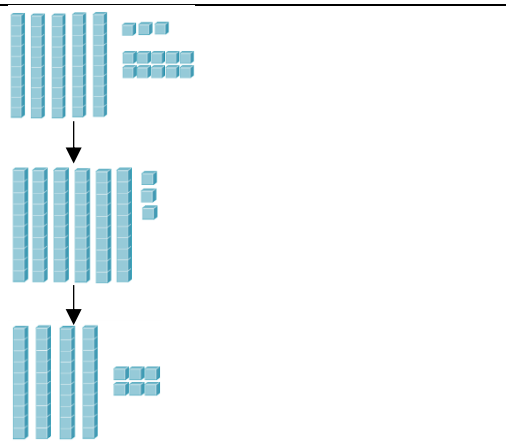
45 - 23 =  
 45 - 20 = 25  
 25 - 3 = 22

67 - 34 = 33

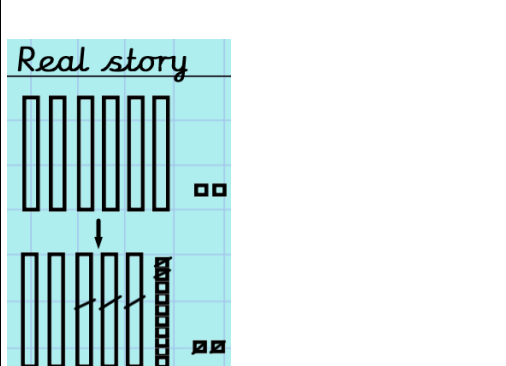


- 45 - 20 - 3 = 25 - 3 = 22
- 45 - 23 = 45 - 20 - 3 = 25 - 3 = 22

First I subtract the tens, then I subtract the ones.

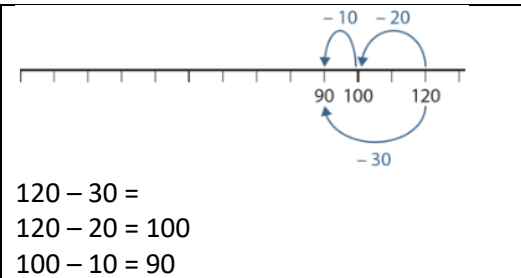
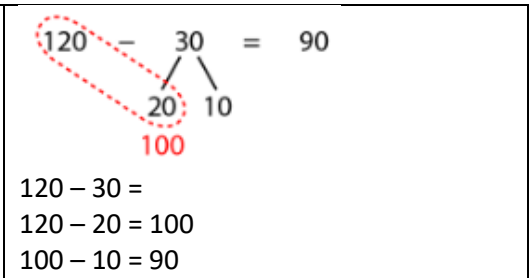
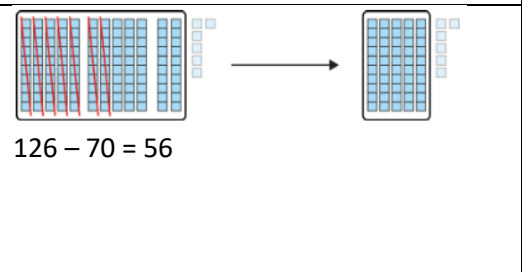
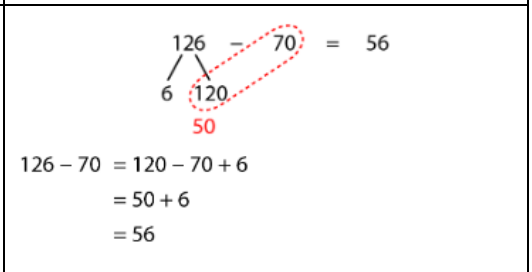
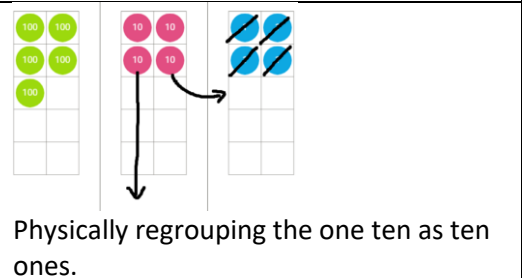
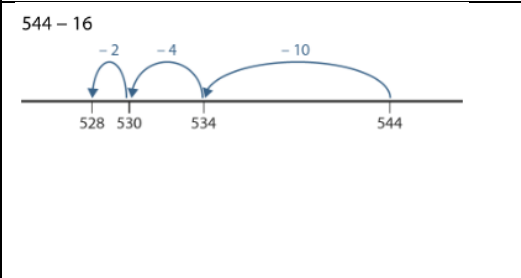
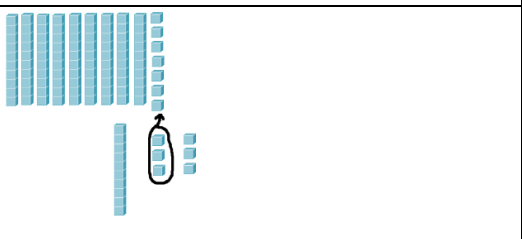
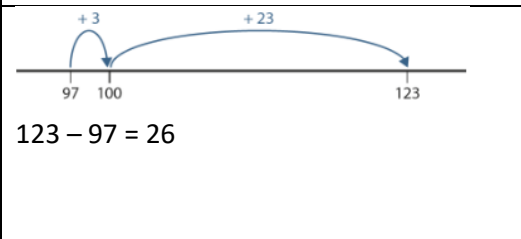


62 - 34 = 28

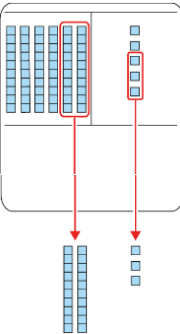
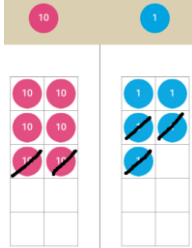
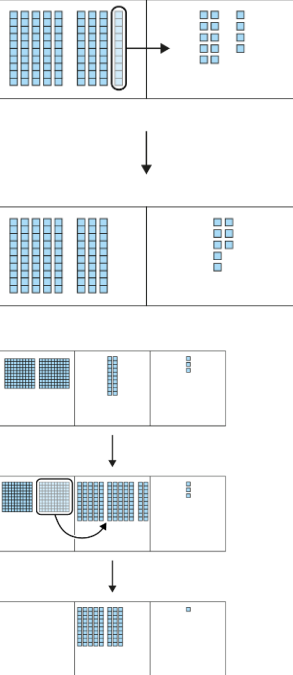
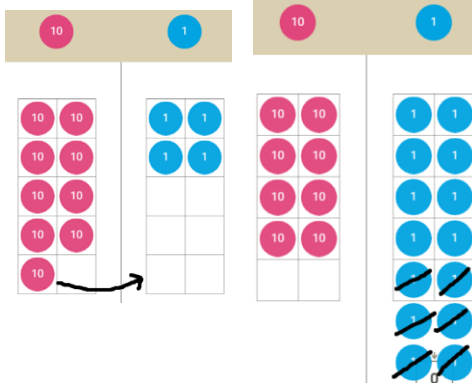


63 - 17 = 46  
 63 - 10 = 53  
 53 - 7 = 53 - 3 - 4 = 46

**Year 2: Bridging**

<p>I know that ___ minus ___ is equal to ___. (bridging ten) So ___ tens minus ___ tens is equal to ___ tens. (bridging ten tens) One hundred and ___ minus ___ is equal to ___.</p> <p><b>Year 3</b></p>	<p>See Year 2 (bridging)</p> 	$120 - 30 =$ $120 - 20 = 100$ $100 - 10 = 90$	 $120 - 30 =$ $120 - 20 = 100$ $100 - 10 = 90$
<p>I know that ___ minus ___ is equal to ___. (bridging ten) So ___ tens minus ___ tens is equal to ___ tens. (bridging ten tens) One hundred and ___ minus ___ is equal to ___.</p> <p><b>Year 3</b></p>	 $126 - 70 = 56$		 $126 - 70 = 120 - 70 + 6$ $= 50 + 6$ $= 56$
<p>We partition the ___ into ___ and ___. First we subtract the ___ from ___ to get to a multiple of 10. Then we subtract the remaining ___ from the multiple of 10. We know 10 minus ___ is equal to ___ so ___ minus ___ is equal to ___.</p> <p><b>Year 3</b></p>	 <p>Physically regrouping the one ten as ten ones.</p>	$544 - 16 =$ 	$544 - 16 =$ $544 - 10 = 534$ $534 - 4 - 2 = 528$
<p>We partition the ___ into ___ and ___. First we add the ___ to ___ to get to 100. Then we add the remaining ___ to 100. We know 100 plus ___ is equal to ___.</p> <p><b>Year 3</b></p>		 $123 - 97 = 26$	<p>As counting up</p> $97 + 3 + 20 + 3 = 123$

## Subtraction: Written Methods

Stem sentences	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)																																																				
<p style="color: red;">We line up the ones; ___ ones plus ___ ones.                      We line up the tens: ___ tens plus ___ tens.                      The ___ is in the ones column – it represents ___ ones.                      ___ ones minus ___ ones is equal to ___ ones.                      The ___ is in the tens column – it represents ___ tens.                      ___ tens minus ___ tens is equal to ___ tens.                      In column subtraction we start at the right-hand side.</p> <p><b>Year 3: Column subtraction of 2 and 3 digit amounts</b></p>		<p>Children could draw place value counters.</p> 	$\begin{array}{r} 65 \\ - 23 \\ \hline 42 \end{array}$ $\begin{array}{r} 462 \\ - 251 \\ \hline \end{array}$																																																				
<p style="color: red;">If there is an insufficient number to subtract from in a given column, we must exchange from the column to the left.</p> <p><b>Year 3: Column Subtraction: Including regrouping digits</b></p>		<p>Children could draw place value counters.</p> 	<table style="margin-left: auto; margin-right: auto;"> <tr><td style="border: 1px solid black; padding: 2px;">10s</td><td style="border: 1px solid black; padding: 2px;">1s</td></tr> <tr><td style="border: 1px solid black; padding: 2px;">9</td><td style="border: 1px solid black; padding: 2px;">14</td></tr> <tr><td style="border: 1px solid black; padding: 2px;">-</td><td style="border: 1px solid black; padding: 2px;">6</td></tr> <tr><td style="border: 1px solid black; padding: 2px;"> </td><td style="border: 1px solid black; padding: 2px;"> </td></tr> </table> <table style="margin-left: auto; margin-right: auto;"> <tr><td style="border: 1px solid black; padding: 2px;">10s</td><td style="border: 1px solid black; padding: 2px;">1s</td></tr> <tr><td style="border: 1px solid black; padding: 2px;">9</td><td style="border: 1px solid black; padding: 2px;">14</td></tr> <tr><td style="border: 1px solid black; padding: 2px;">-</td><td style="border: 1px solid black; padding: 2px;">6</td></tr> <tr><td style="border: 1px solid black; padding: 2px;">8</td><td style="border: 1px solid black; padding: 2px;">8</td></tr> </table> <table style="margin-left: auto; margin-right: auto; font-size: small;"> <tr><td style="border: 1px solid black; padding: 2px;">100s</td><td style="border: 1px solid black; padding: 2px;">10s</td><td style="border: 1px solid black; padding: 2px;">1s</td></tr> <tr><td style="border: 1px solid black; padding: 2px;">2</td><td style="border: 1px solid black; padding: 2px;">2</td><td style="border: 1px solid black; padding: 2px;">3</td></tr> <tr><td style="border: 1px solid black; padding: 2px;">-</td><td style="border: 1px solid black; padding: 2px;">1</td><td style="border: 1px solid black; padding: 2px;">4</td></tr> <tr><td style="border: 1px solid black; padding: 2px;"> </td><td style="border: 1px solid black; padding: 2px;"> </td><td style="border: 1px solid black; padding: 2px;"> </td></tr> </table> <table style="margin-left: auto; margin-right: auto; font-size: small;"> <tr><td style="border: 1px solid black; padding: 2px;">100s</td><td style="border: 1px solid black; padding: 2px;">10s</td><td style="border: 1px solid black; padding: 2px;">1s</td></tr> <tr><td style="border: 1px solid black; padding: 2px;"><del>2</del></td><td style="border: 1px solid black; padding: 2px;">12</td><td style="border: 1px solid black; padding: 2px;">3</td></tr> <tr><td style="border: 1px solid black; padding: 2px;">-</td><td style="border: 1px solid black; padding: 2px;">1</td><td style="border: 1px solid black; padding: 2px;">4</td></tr> <tr><td style="border: 1px solid black; padding: 2px;"> </td><td style="border: 1px solid black; padding: 2px;"> </td><td style="border: 1px solid black; padding: 2px;"> </td></tr> </table> <table style="margin-left: auto; margin-right: auto; font-size: small;"> <tr><td style="border: 1px solid black; padding: 2px;">100s</td><td style="border: 1px solid black; padding: 2px;">10s</td><td style="border: 1px solid black; padding: 2px;">1s</td></tr> <tr><td style="border: 1px solid black; padding: 2px;"><del>2</del></td><td style="border: 1px solid black; padding: 2px;">12</td><td style="border: 1px solid black; padding: 2px;">3</td></tr> <tr><td style="border: 1px solid black; padding: 2px;">-</td><td style="border: 1px solid black; padding: 2px;">1</td><td style="border: 1px solid black; padding: 2px;">4</td></tr> <tr><td style="border: 1px solid black; padding: 2px;">0</td><td style="border: 1px solid black; padding: 2px;">8</td><td style="border: 1px solid black; padding: 2px;">1</td></tr> </table>	10s	1s	9	14	-	6			10s	1s	9	14	-	6	8	8	100s	10s	1s	2	2	3	-	1	4				100s	10s	1s	<del>2</del>	12	3	-	1	4				100s	10s	1s	<del>2</del>	12	3	-	1	4	0	8	1
10s	1s																																																						
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-	1	4																																																					
0	8	1																																																					

If there is an insufficient number to subtract from in a given column, we must exchange from the column to the left.

**Year 4, 5 and 6**

See Year 3 examples

See Year 3 examples

$$\begin{array}{r} \overset{5}{\cancel{6}}, \overset{14}{\cancel{5}} \overset{12}{\cancel{3}} \overset{1}{8} \\ - 2, 7 \ 8 \ 9 \\ \hline 3, 7 \ 4 \ 9 \end{array}$$

$$\begin{array}{r} \pounds \ 2 \ \overset{8}{\cancel{9}} \ . \ \overset{14}{\cancel{5}} \ 0 \\ - \pounds \ 1 \ 8 \ . \ 9 \ 4 \\ \hline \pounds \ 1 \ 0 \ . \ 5 \ 6 \end{array}$$

# Subtraction Known Number Facts

KS1

-	0	1	2	3	4	5	6	7	8	9	10
0	0-0										
1	1-0	1-1									
2	2-0	2-1	2-2								
3	3-0	3-1	3-2	3-3							
4	4-0	4-1	4-2	4-3	4-4						
5	5-0	5-1	5-2	5-3	5-4	5-5					
6	6-0	6-1	6-2	6-3	6-4	6-5	6-6				
7	7-0	7-1	7-2	7-3	7-4	7-5	7-6	7-7			
8	8-0	8-1	8-2	8-3	8-4	8-5	8-6	8-7	8-8		
9	9-0	9-1	9-2	9-3	9-4	9-5	9-6	9-7	9-8	9-9	
10	10-0	10-1	10-2	10-3	10-4	10-5	10-6	10-7	10-8	10-9	10-10
11		11-1	11-2	11-3	11-4	11-5	11-6	11-7	11-8	11-9	11-10
12			12-2	12-3	12-4	12-5	12-6	12-7	12-8	12-9	12-10
13				13-3	13-4	13-5	13-6	13-7	13-8	13-9	13-10
14					14-4	14-5	14-6	14-7	14-8	14-9	14-10
15						15-5	15-6	15-7	15-8	15-9	15-10
16							16-6	16-7	16-8	16-9	16-10
17								17-7	17-8	17-9	17-10
18									18-8	18-9	18-10
19										19-9	19-10
20											20-10

**One More, One Less**

**Two More, Two Less: Think Odds and Evens**

**Number 10 Fact Families**

**Five and A Bit**

**Know About Zero**

**Doubles and Near Doubles**

**Number Neighbours: Spot the Difference**

**7 Tree 9 Square**

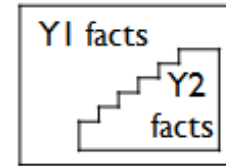
**Ten and A Bit**

**Make 10 and Then**

**Adjusting**

**Suap It**

1 + 6



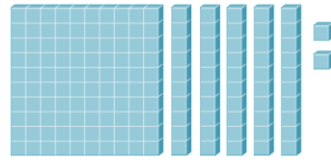
KS2

Strategy	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)
Bridging through a multiple of 10, 100, etc  <b>Years 3, 4, 5 and 6</b>	<p>12 - 4 = 12 - 2 = 10 10 - 2 = 8</p>	<p>120 - 30 = 120 - 20 = 100 100 - 10 = 90</p>	<p>120 - 30 = 120 - 20 = 100 100 - 10 = 90</p>

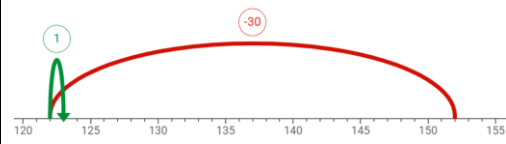
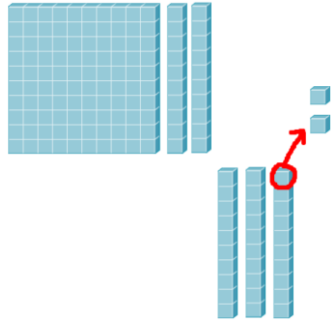


Compensating – rounding to the nearest multiple 10, 100, etc and adjusting

**Years 3, 4, 5 and 6**



$$152 - 29$$



$$152 - 30 = 122$$

$$122 + 1 = 123$$

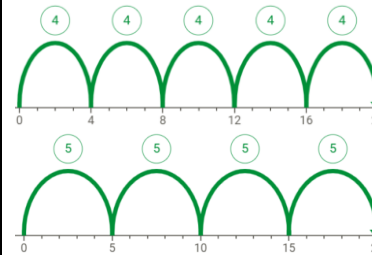
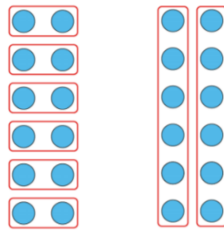
## Multiplication

Stem sentences	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)
<p>One group of two, two groups of two, three groups of 2, ...</p> <p>Ten, twenty, thirty, ...</p> <p>One five, two fives, three fives, ...</p> <p><b>Year 1</b></p>	<p>two      four      six      eight      ten</p> <p>2          4          6          8          10</p>		<p>10, 20, 30, ...</p>
<p>There are __ coins.</p> <p>Each coin has a value of __p.</p> <p>This is __p.</p> <p><b>Year 1</b></p>	<p>Representing each group by one object</p>		<p>Five 2p coins = 10p</p>
<p>There are ____ equal groups</p> <p>There are ____ in each group</p> <p><b>Year 2</b></p>			<p><math>5 + 5 + 5</math></p>
<p>There are __ in each group.</p> <p>There are __ groups.</p> <p>There are __ in a group and __ groups.</p> <p><b>Year 2</b></p>			<p><math>2 + 2 + 2 + 2 = 8</math></p> <p><math>2 \times 4 = 8</math></p> <p><math>5 + 5 + 5 = 15</math></p> <p><math>5 \times 3 = 15</math></p>
<p>Factor times factor is equal to the product.</p> <p>The product is equal to factor times factor.</p> <p><b>Year 2</b></p>	<p>Unitising equal groups – representing each group by one object</p>		<p><math>2 \times 3 = 6</math></p> <p><math>6 = 2 \times 3</math></p>

\_\_ times \_\_ can represent \_\_ in a group and \_\_ groups.  
It can also represent \_\_ groups of \_\_.

Multiplication is commutative.

**Year 2**



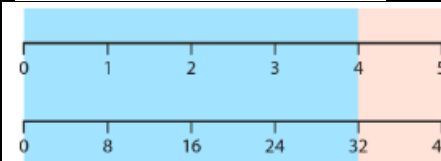
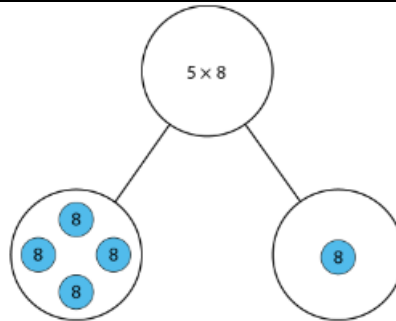
$$2 \times 5 = 5 \times 2$$

\_\_ is equal to \_\_ plus \_\_, so \_\_ times \_\_ is equal to \_\_ times \_\_ plus \_\_ times \_\_.

\_\_ is equal to \_\_ minus \_\_, so \_\_ times \_\_ is equal to \_\_ times \_\_ minus \_\_ times \_\_.

Multiplication is distributive.

**Year 3**



$$\begin{aligned} 5 &= 4 + 1 \\ 5 \times 8 &= 4 \times 8 + 1 \times 8 \\ &= 32 + 8 \\ &= 40 \end{aligned}$$

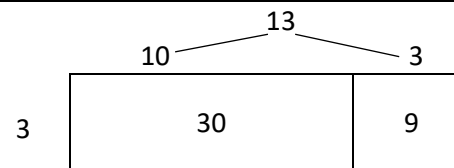
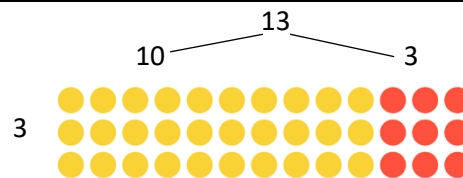
$$\begin{aligned} 4 &= 5 - 1 \\ 4 \times 8 &= 5 \times 8 - 1 \times 8 \\ &= 40 - 8 \\ &= 32 \end{aligned}$$

\_\_ is equal to \_\_ plus \_\_, so \_\_ times \_\_ is equal to \_\_ times \_\_ plus \_\_ times \_\_.

\_\_ is equal to \_\_ minus \_\_, so \_\_ times \_\_ is equal to \_\_ times \_\_ minus \_\_ times \_\_.

Multiplication is distributive.

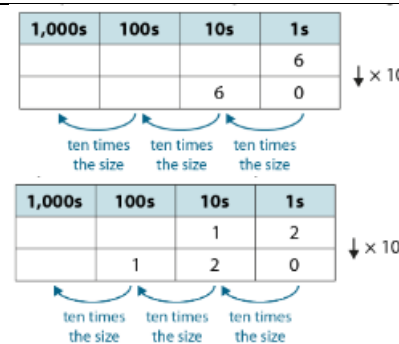
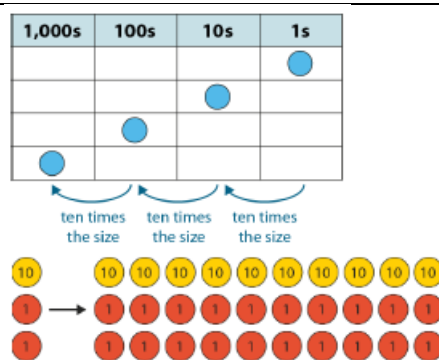
**Year 3**



$$\begin{aligned} 3 \times 13 &= 3 \times 10 + 3 \times 3 \\ &= 30 + 9 \\ &= 39 \end{aligned}$$

To multiply a whole number by 10, the digits move one place to the left and add a zero place holder.

**Year 3**

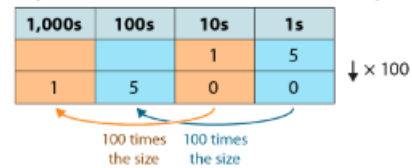
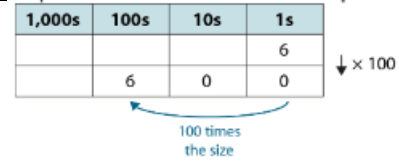
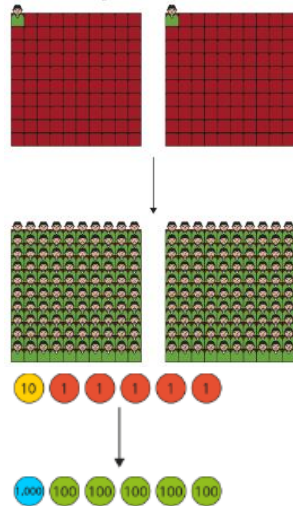


$$6 \times 10 = 60$$

$$12 \times 10 = 120$$

All multiples of 100 have both a tens and ones digit of 0.  
When a number is multiplied by 100, the product is a multiple of 100.

**Year 3**



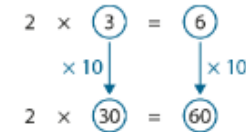
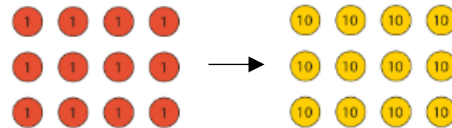
$2 \times 100 = 200$   
There are 100 times as many people as before.

$15 \times 100 = 1500$

If one factor is made ten times the size, the product will be ten times the size.

3 times 5 is equal to 15.” “3 times 5 tens is equal to 15 tens.” “15 tens is equal to 150.”

**Year 3**

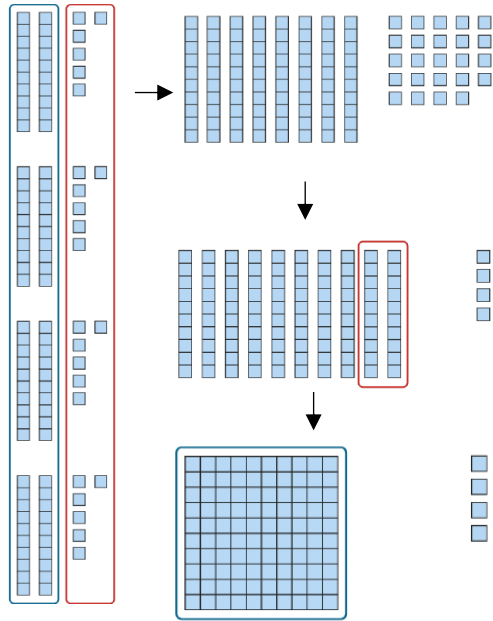


$4 \times 3 = 12$  so  $4 \times 30 = 120$

If there are ten or more ones, we must regroup the ones into tens and ones.  
If there are ten or more tens, we must regroup the tens into hundreds and tens.

Multiplication is distributive. Informal multiplication of 2 or 3 digit amounts

**Year 4**



$$\begin{array}{r} 84 \\ \times 6 \\ \hline 504 \end{array}$$

$84 \times 6 = 504$

$84$  is decomposed into  $80$  and  $4$ .

$$80 \times 6 = 480$$
$$4 \times 6 = 24$$
$$480 + 24 = 504$$

$$84 \times 6 = 80 \times 6 + 4 \times 6$$
$$= 480 + 24$$
$$= 504$$

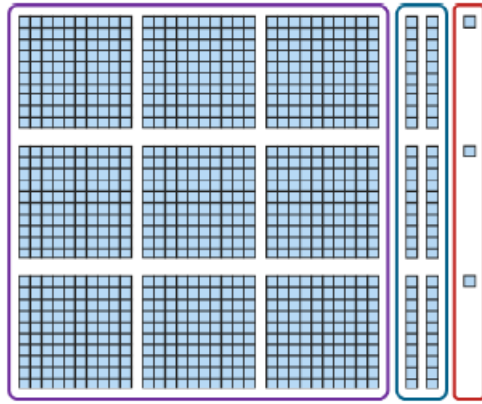
## Multiplication: Formal Written Methods

Stem sentences	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)																														
<p style="color: red;">We work from the least significant digit, on the right, to the most significant digit, on the left.</p> <p>Multiplication is distributive.</p> <p><b>Year 5</b></p>		<p><math>34 \times 2 = 60 + 8 = 68</math></p>	<table style="margin-left: auto; margin-right: auto;"> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">10s</td><td style="padding: 2px 5px;">1s</td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">3</td><td style="padding: 2px 5px;">4</td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">×</td><td style="padding: 2px 5px;">2</td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;"></td><td style="padding: 2px 5px;">8</td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">6</td><td style="padding: 2px 5px;">0</td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">6</td><td style="padding: 2px 5px;">8</td></tr> </table> <p style="text-align: center;">↓</p> <table style="margin-left: auto; margin-right: auto;"> <tr><td style="padding: 2px 5px;">2</td><td style="padding: 2px 5px;">1</td></tr> <tr><td style="padding: 2px 5px;">×</td><td style="padding: 2px 5px;">4</td></tr> <tr><td style="padding: 2px 5px;">8</td><td style="padding: 2px 5px;">4</td></tr> </table> <p style="margin-left: 100px; color: red;">2 × 4 ones = 8 ones</p> <p style="margin-left: 100px; color: blue;">2 × 3 tens = 6 tens</p>	10s	1s	3	4	×	2		8	6	0	6	8	2	1	×	4	8	4												
10s	1s																																
3	4																																
×	2																																
	8																																
6	0																																
6	8																																
2	1																																
×	4																																
8	4																																
<p style="color: red;">If there are ten or more ones, we must regroup the ones into tens and ones. If there are ten or more tens, we must regroup the tens into hundreds and tens.</p> <p>Multiplication is distributive.</p> <p><b>Year 5</b></p>		<p><math>24 \times 3 = 60 + 12 = 72</math></p>	<table style="margin-left: auto; margin-right: auto;"> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">10s</td><td style="padding: 2px 5px;">1s</td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">2</td><td style="padding: 2px 5px;">4</td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">×</td><td style="padding: 2px 5px;">3</td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">1</td><td style="padding: 2px 5px;">2</td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">6</td><td style="padding: 2px 5px;">0</td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">7</td><td style="padding: 2px 5px;">2</td></tr> </table> <p style="text-align: center;">↓</p> <table style="margin-left: auto; margin-right: auto;"> <tr><td style="padding: 2px 5px;">1</td><td style="padding: 2px 5px;">8</td></tr> <tr><td style="padding: 2px 5px;">×</td><td style="padding: 2px 5px;">5</td></tr> <tr><td style="padding: 2px 5px;">9</td><td style="padding: 2px 5px;">0</td></tr> <tr><td style="padding: 2px 5px;">4</td><td style="padding: 2px 5px;"></td></tr> </table> <table style="margin-left: 100px; margin-right: auto;"> <tr><td style="padding: 2px 5px;">3</td><td style="padding: 2px 5px;">8</td></tr> <tr><td style="padding: 2px 5px;">×</td><td style="padding: 2px 5px;">4</td></tr> <tr><td style="padding: 2px 5px;">1</td><td style="padding: 2px 5px;">5</td></tr> <tr><td style="padding: 2px 5px;">2</td><td style="padding: 2px 5px;">2</td></tr> <tr><td style="padding: 2px 5px;">3</td><td style="padding: 2px 5px;"></td></tr> </table> <p style="margin-left: 100px; color: red;">3 × 4 ones = 12 ones = 1 ten + 2 ones</p> <p style="margin-left: 100px; color: blue;">3 × 2 tens = 6 tens</p>	10s	1s	2	4	×	3	1	2	6	0	7	2	1	8	×	5	9	0	4		3	8	×	4	1	5	2	2	3	
10s	1s																																
2	4																																
×	3																																
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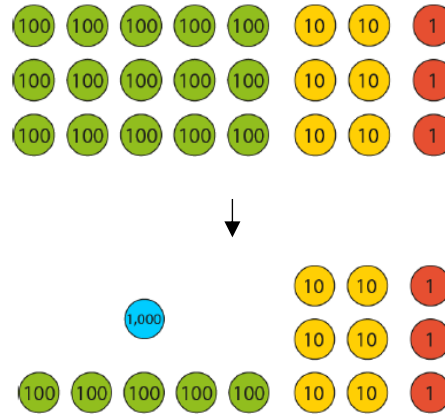
If there are ten or more ones, we must regroup the ones into tens and ones.  
 If there are ten or more tens, we must regroup the tens into hundreds and tens.  
 If there are ten or more hundreds, we must regroup the hundreds into thousands and hundred.

Multiplication is distributive.

**Year 5**



$321 \times 3 = 963$



$521 \times 3 = 1000 + 500 + 60 + 3 = 1563$

100s	10s	1s
3	2	1
×		
		3
	6	0
9	0	0
9	6	3

$3 \times 1 \text{ ones} = 3 \text{ ones}$   
 $3 \times 2 \text{ tens} = 6 \text{ tens}$   
 $3 \times 3 \text{ hundreds} = 9 \text{ hundreds}$

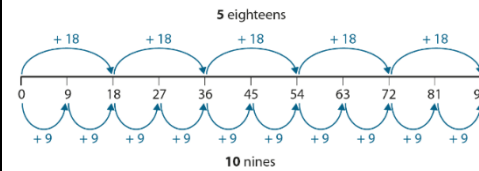
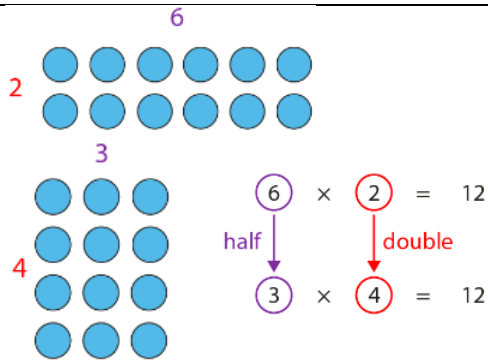
3	2	1
×		
		3
9	6	3

1,000s	100s	10s	1s
	5	2	1
×			
			3
		6	0
1	5	0	0
1	5	6	3
3 6 7			
×			
			4
	1	4	6 8
	2	2	

If there is a multiplicative increase in one factor and a multiplicative decrease in the other, the product remains the same.

If I multiply one factor by \_\_, I must divide the other factor by \_\_ for the product to remain the same.

**Year 5 and 6**

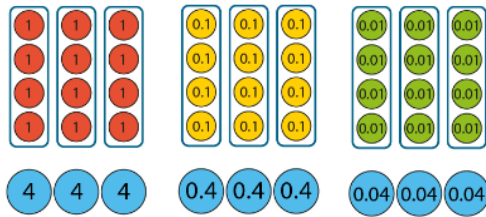


$2 \times 9 = 18$   
 $\times 3 \downarrow \div 3$   
 $6 \times 3 = 18$

If one factor is made one tenth of the size, the product will be one tenth of the size.

If one factor is made one hundredth of the size, the product will be one hundredth of the size.

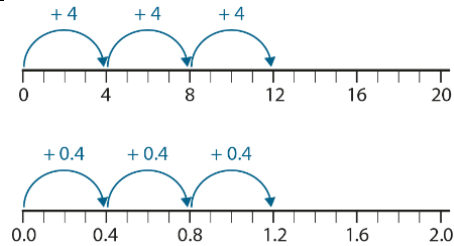
I move the digits of the number I am multiplying \_\_\_ places to the left until I get a whole number; then I multiply; then I move the digits of the product \_\_\_ places to the right.



$$4 \times 3 = 12$$

$$0.4 \times 3 = 1.2$$

$$0.04 \times 3 = 0.12$$



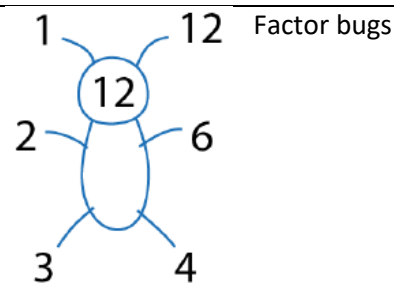
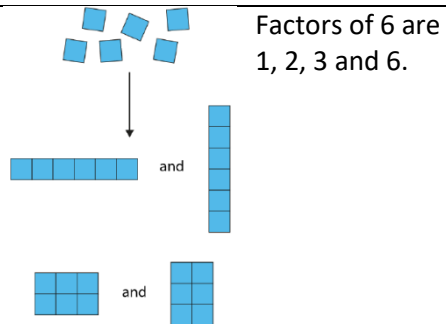
$$\begin{array}{r} 4 \ 5 \ 6 \\ \times \quad \quad 4 \\ \hline 1 \ 8 \ 2 \ 4 \\ 2 \ 2 \phantom{0} \\ \hline \end{array}$$
  

$$\begin{array}{r} 4 \ . \ 5 \ 6 \\ \times \quad \quad 4 \\ \hline 1 \ 8 \ . \ 2 \ 4 \\ 2 \ 2 \phantom{0} \\ \hline \end{array}$$

**Year 5**

Numbers that have more than two factors are composite numbers.

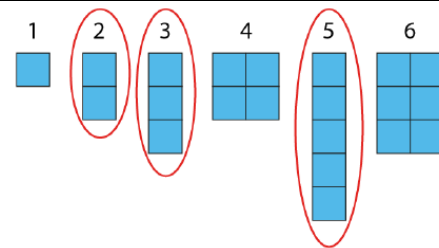
**Year 5**



Factors of 6 are 1, 2, 3 and 6.

Numbers that have only two factors are prime numbers.

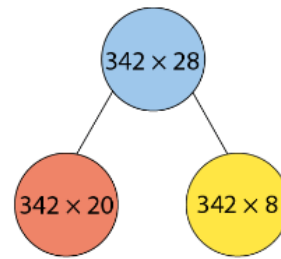
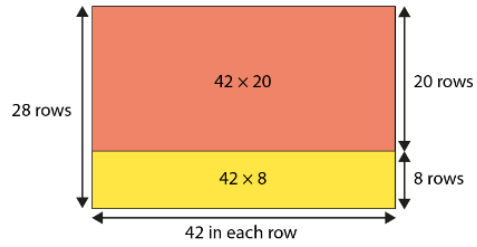
**Year 5**



17 is a prime number because its only factors are 1 and 17.



To multiply two two-digit numbers, first multiply by the ones, then multiply by the tens, then add them together.  
 To multiply a three-digit number by a two-digit number, first multiply by the ones, then multiply by the tens, then add them together.



	100s	10s	1s	
×	2	7		
	2	3		
	8	1	27 × 3	
	5	4	0	27 × 20
	6	2	1	
	1			

		3	1	2
×		2	8	
	2	4	9	6
	6	2	4	0
	8	7	3	6
				1

**Year 6**

## Multiplication – Key mental strategies for Key Stage 2

Children are taught automatic recall of the times table facts through a variety of methods. This includes ‘rolling numbers’ beginning with 2, 5 and 10 in Year 1 and 2 And 3, 4, 5, 6, 7, 8 and 9 from Year 3 onwards.

Quick recall of times table facts upto 12 x 12 is practised daily through discrete activities. Alongside this the maths lesson should be used to gain clear conceptual knowledge as detailed above.

In Year 3, children will practice their automatic recall of facts in the 2, 5, 10, 3 and 4 times table. In Year 4 this will be extended to the 6, 7, 8, 9, 11 and 12 times table. Strategies to quickly derive the 11 and 12 times table will also be explored.

The national curriculum requires pupils to recall multiplication table facts up to  $12 \times 12$ , and this is assessed in the multiplication tables check. For pupils who do not have automatic recall of all of the facts by the time of the check, fluency in facts up to  $9 \times 9$  should be prioritised in the remaining part of year 4. The facts to  $9 \times 9$  are particularly important for progression to year 5, because they are required for formal written multiplication and division.

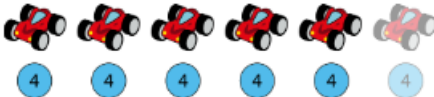
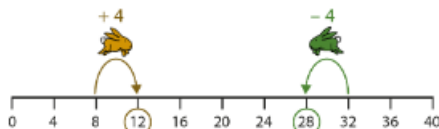
The 36 multiplication facts that are required for formal written multiplication are as follows.

$2 \times 2$								
$3 \times 2$	$3 \times 3$							
$4 \times 2$	$4 \times 3$	$4 \times 4$						
$5 \times 2$	$5 \times 3$	$5 \times 4$	$5 \times 5$					
$6 \times 2$	$6 \times 3$	$6 \times 4$	$6 \times 5$	$6 \times 6$				
$7 \times 2$	$7 \times 3$	$7 \times 4$	$7 \times 5$	$7 \times 6$	$7 \times 7$			
$8 \times 2$	$8 \times 3$	$8 \times 4$	$8 \times 5$	$8 \times 6$	$8 \times 7$	$8 \times 8$		
$9 \times 2$	$9 \times 3$	$9 \times 4$	$9 \times 5$	$9 \times 6$	$9 \times 7$	$9 \times 8$	$9 \times 9$	

During application of formal written multiplication, pupils may also need to multiply a one-digit number by 1. Multiplication of the numbers 1 to 9 by 1 are not listed here because these calculations do not need to be recalled in the same way.

While pupils are learning the individual multiplication tables, they should also learn that:

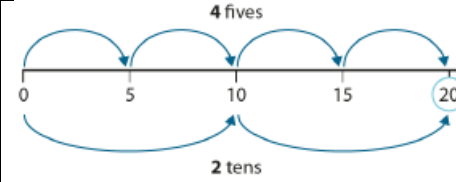
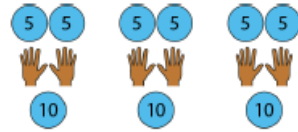
- the factors can be written in either order and the product remains the same (for example, we can write  $3 \times 4 = 12$  or  $4 \times 3 = 12$  to represent the third fact in the 4 multiplication table)
- the products within each multiplication table are multiples of the corresponding number, and be able to recognise multiples (for example, pupils should recognise, 64 is a multiple of 8, but that 68 is not)

Strategy	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)
Adjacent multiples of ___ have a difference of ___.  <b>Year 3 onwards</b>			$4 \times 6 = 4 \times 5 + 4$  $4 \times 9 = 4 \times 10 - 4$

Products in the 10 times table are double the products in the 5 times table.  
Products in the 5 times table are half of the products in the 10 times table.

(NCETM Year 2 unit 2.5)

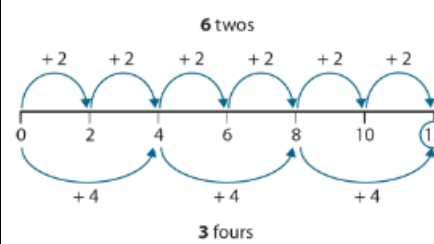
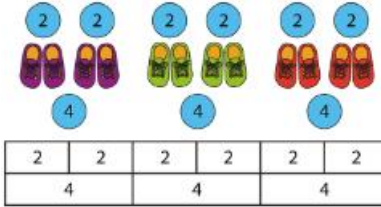
**Year 2 onwards**



$$5 \times 4 = 10 \times 2$$

Products in the 4 times table are double the products in the 2 times table.  
Products in the 2 times table are half of the products in the 4 times table.

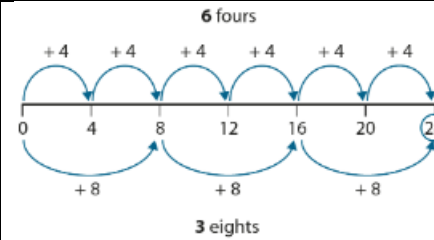
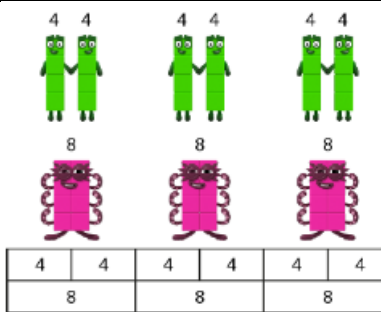
**Year 3 onwards**



$$2 \times 6 = 4 \times 3$$

Products in the 8 times table are double the products in the 4 times table.  
Products in the 4 times table are half of the products in the 8 times table.

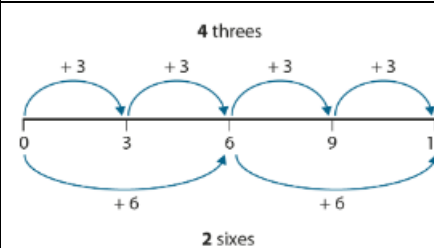
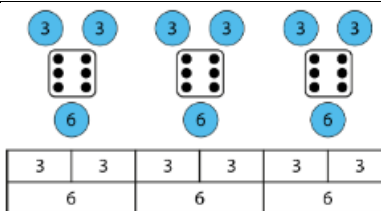
**Year 3 onwards**



$$4 \times 6 = 8 \times 3$$

Products in the 6 times table are double the products in the 3 times table.  
Products in the 3 times table are half of the products in the 6 times table.





**Year 3 onwards**



$$3 \times 4 = 6 \times 2$$







When both factors are odd, the product is odd.  
 When one factor is odd and the other factor is even, the product is even.

**Year 4 onwards**

	$1 \times 7 = 7$	$7 \times 1 = 7$
odd	odd	odd
	$2 \times 7 = 14$	$7 \times 2 = 14$
even	odd	even
	$3 \times 7 = 21$	$7 \times 3 = 21$
odd	odd	odd
	$4 \times 7 = 28$	$7 \times 4 = 28$
even	odd	even

odd x odd = odd  
 odd x even = even  
 even x odd = even  
 even x even = even

Products in the 9 times table are triple the products in the 3 times table.

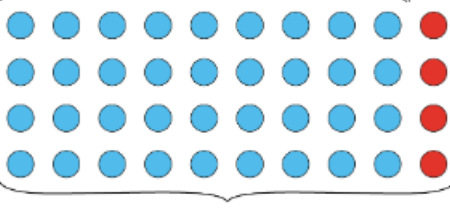
		
3	3	3
		
9	9	9
3	3	3
9	9	9



$3 \times 12 = 9 \times 4$

Products in the 10 times table can be used to find products in the 9 times table.

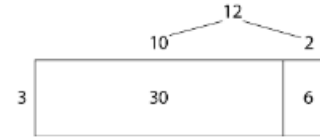
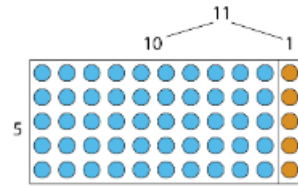
**Year 3 onwards**



$9 \times 4 = 10 \times 4 - 1 \times 4$


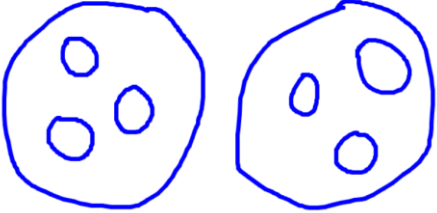

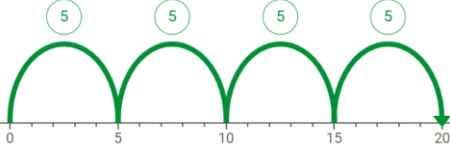

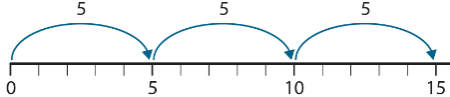
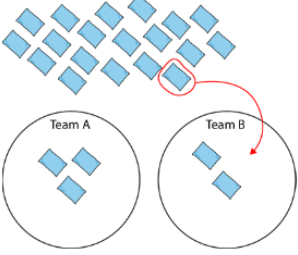
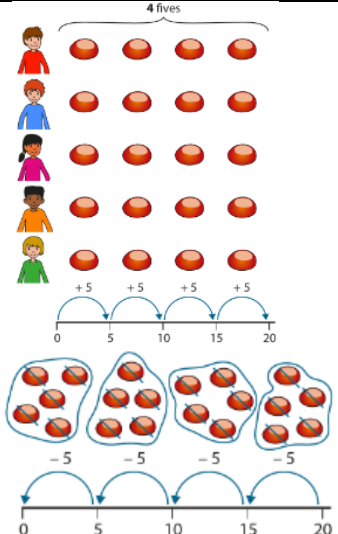
Products in the 10 times table can be used to find products in the 11 times table and 12 times table.

**Year 4 onwards**



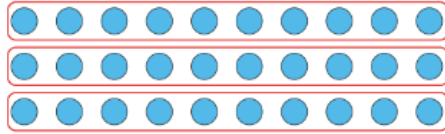
$$\begin{aligned} 12 \times 3 &= 10 \times 3 + 2 \times 3 \\ &= 30 + 6 \\ &= 36 \end{aligned}$$

## Division

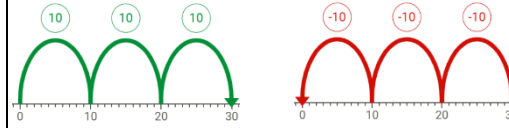
Stem sentences	Concrete (Can we make it?)	Pictorial (Can we draw it?)	Abstract (Can we write the equation?)
<p>One group of two, two groups of two, three groups of 2, ...</p> <p>Ten, twenty, thirty, ...</p> <p>One five, two fives, three fives, ...</p> <p><b>Year 1</b></p>			<p>6 biscuits shared between 2 children gives 3 biscuits each.</p>
<p>The ____ costs __p.</p> <p>Each coin has a value of __p.</p> <p>So I need __ coins.</p> <p><b>Year 1</b></p>			<p>Five 2p coins = 10p</p>
<p>__ is divided into groups of __.</p> <p>There are __ groups.</p> <p>We can skip count using the divisor to find the quotient.</p> <p><b>Year 2</b></p>			<p><math>5 + 5 + 5 = 15</math></p> <p><math>15 \div 5 = 3</math></p>
<p>__ divided between __ is equal to __ each.</p> <p>We can skip count using the divisor to find the quotient.</p> <p><b>Year 2</b></p>			<p>One 5 is 1 each. That's 5.</p> <p>Two 5s is 2 each. That's 10.</p> <p><math>10 \div 5 = 2</math></p>

Ten times    is equal to    so    divided into groups of ten is   .

**Year 2**



30 represents the total number of counters.  
10 represents the number in each group.  
3 represents the number of groups.



$10 \times 3 = 30$   
 $3 \times 10 = 30$   
 $30 \div 10 = 3$

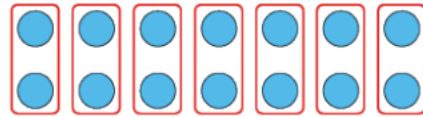
Answers can be derived by skip counting

   twos are 14. 7 twos are 14.  
   times    is 14, so 14 divided by 2 is   ." "14 divided into groups of 2 is equal to   ."

If the divisor is   , we can use the    times table to find the quotient.

**Year 3**

I need 14 ping-pong balls. There are 2 ping-pong balls in a pack. How many packs do I need?



$14 \div 2 = 7$

14						
2	2	2	2	2	2	2

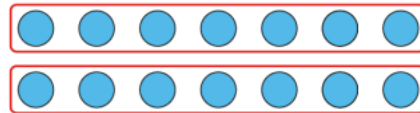
$14 \div 2 = 7$

Answers should be derived using known multiplication facts

   twos are 14. 7 twos are 14.  
   times    is 14, so 14 divided by 2 is   ." "£14 shared between 2 is equal to £7 each.

If the divisor is   , we can use the    times table to find the quotient.

£14 is shared between 2 children. How much money does each child get?



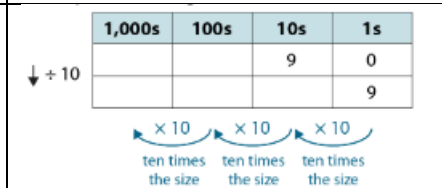
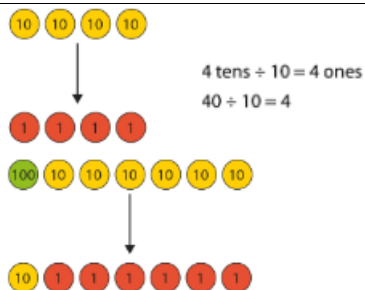
14	
7	7

$14 \div 2 = 7$

Answers should be derived using known multiplication facts

To divide a multiple of ten by 10, remove the zero from the ones place.

**Year 3**



$90 \div 10 = 9$

$150 \div 10 = 15$

To divide a multiple of 100 by 100, remove two zeros (from the tens and ones places).

Year 3

100 times as many

$\times 100$

$\square \times 100 = 200$        $200 \div 100 = \square$

100 100 100 100 100 100 100

10 1 1 1 1 1 1 1

1,000s	100s	10s	1s
	9	0	0
			9

0 0

100 times the size      100 times the size

$900 \div 100 = 9$

$1500 \div 100 = 15$

If the dividend is made ten times the size, the quotient will be ten times the size.

Year 3

$8 \div 4 = 2$

$80 \div 4 = 20$

$-2$   $-2$   $-2$   $-2$

$-20$   $-20$   $-20$   $-20$

$12 \div 3 = 4$

$\times 10$

$120 \div 3 = 40$

\_\_\_ is divided into groups of \_\_\_. There are \_\_\_ groups and a remainder of \_\_\_.

Year 4

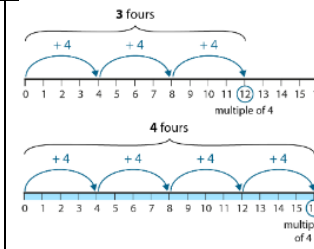
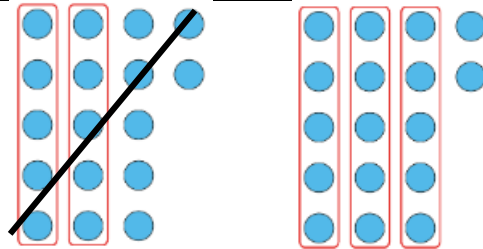
4 4 4

$14 = 4 \times 3 + 2$   
 $14 \div 4 = 3 \text{ r } 2$



\_\_\_ is a multiple of \_\_\_ so when it is divided into groups of \_\_\_, there is no remainder.

The remainder is always less than the divisor.

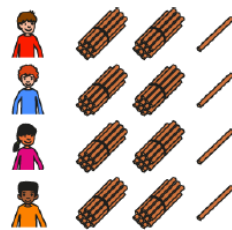


$17 \div 5 = 2 \text{ r } 7$  is incorrect because 7 is greater than 5.

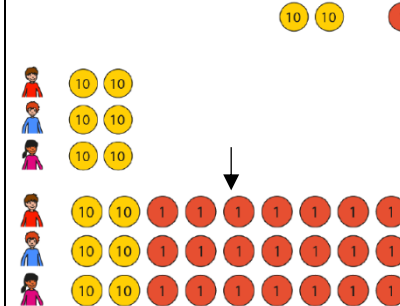
$$17 \div 5 = 3 \text{ r } 2$$

**Year 4**

If dividing the tens gives a remainder of one or more tens, we must exchange the remaining tens for ones.



$$84 \div 4 = 21$$



$$\begin{array}{r} 8 \text{ tens} \div 4 = 2 \text{ tens} \\ 4 \text{ ones} \div 4 = 1 \text{ one} \\ \hline 84 \div 4 = 21 \end{array}$$

$$\begin{array}{r} 6 \text{ tens} \div 3 = 2 \text{ tens} \\ 21 \text{ ones} \div 3 = 7 \text{ ones} \\ \hline 81 \div 3 = 27 \end{array}$$

**Year 4**

### Division: Written Methods

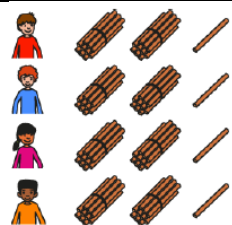
Stem sentences

Concrete (Can we make it?)

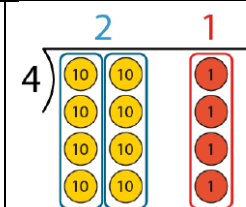
Pictorial (Can we draw it?)

Abstract (Can we write the equation?)

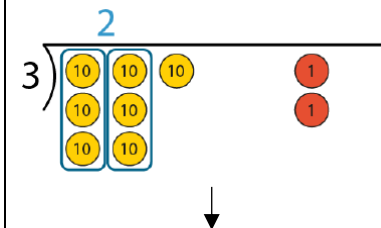
If dividing the tens gives a remainder of one or more tens, we must exchange the remaining tens for ones.



**Year 5**



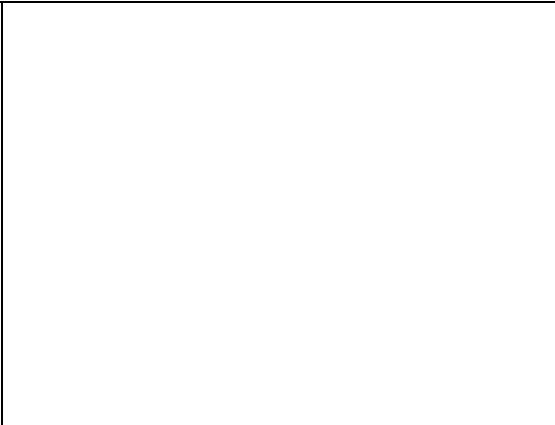
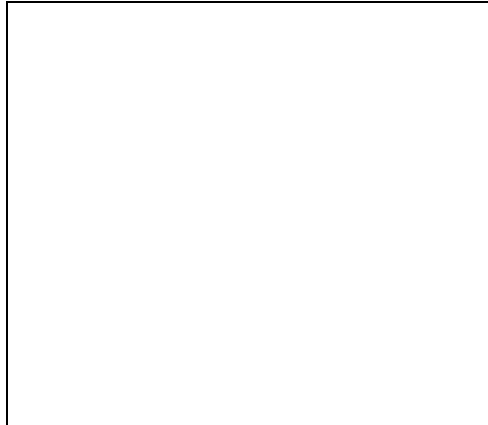
$$72 \div 3 = 24$$



$$\begin{array}{r} 10\text{s} \quad 1\text{s} \\ 2 \quad 1 \\ 4 \overline{) 72} \\ \underline{4} \quad 4 \\ 8 \quad 4 \\ \underline{4} \quad 4 \\ 4 \quad 4 \\ \underline{4} \quad 4 \\ 0 \end{array} \quad \begin{array}{l} 8 \text{ tens} \div 4 = 2 \text{ tens} \\ 4 \text{ ones} \div 4 = 1 \text{ one} \end{array}$$

$$\begin{array}{r} 2 \quad 1 \\ 4 \overline{) 72} \\ \underline{4} \quad 4 \\ 8 \quad 4 \\ \underline{4} \quad 4 \\ 0 \end{array}$$

$$\begin{array}{r} 2 \quad 4 \\ 3 \overline{) 72} \\ \underline{6} \quad 4 \\ 1 \quad 2 \end{array}$$



$$\begin{array}{r} 2 \quad 4 \\ 3 \overline{) 73} \\ \underline{60} \phantom{0} \\ 13 \phantom{0} \\ \underline{12} \\ 1 \end{array}$$

$73 \div 3 = 24 \text{ r } 1$

$$\begin{array}{r} 2 \quad 4 \quad \text{r}1 \\ 3 \overline{) 73} \\ \underline{60} \phantom{0} \\ 13 \phantom{0} \\ \underline{12} \\ 1 \end{array}$$

$$\begin{array}{r} 2 \quad 4 \text{ r}1 \\ 3 \overline{) 73} \end{array}$$

If dividing the hundreds gives a remainder of one or more hundreds, we must exchange the remaining hundreds for tens.

**Year 5**

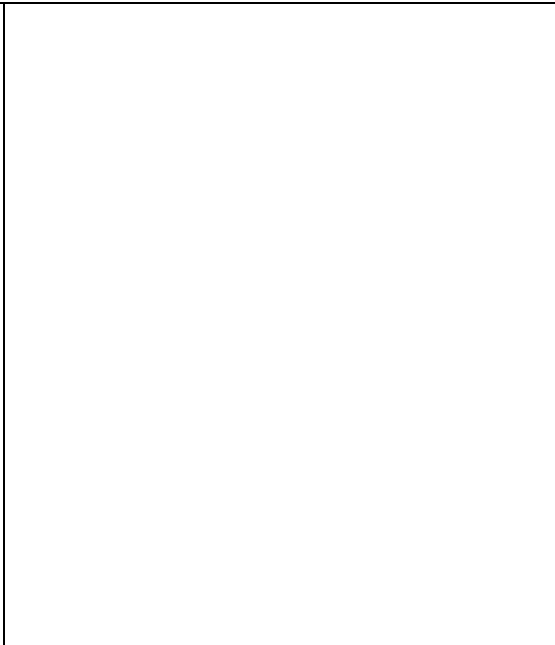
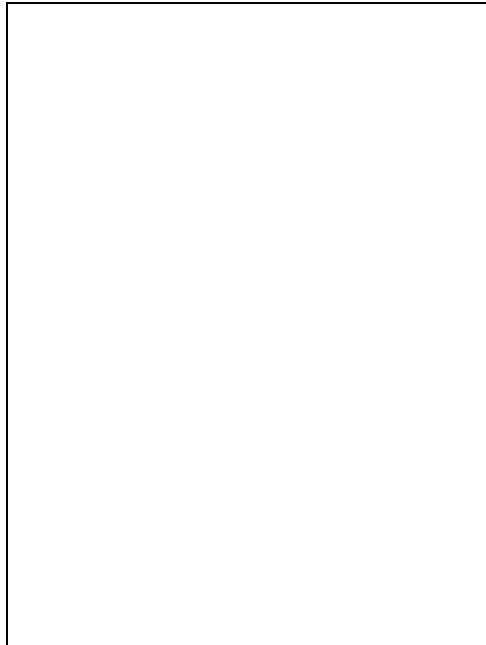
$$\begin{array}{r} 2 \quad 1 \quad 2 \\ 4 \overline{) 848} \\ \underline{800} \phantom{0} \\ 48 \phantom{0} \\ \underline{40} \phantom{0} \\ 88 \\ \underline{80} \\ 8 \end{array}$$

$$\begin{array}{r} 1 \\ 5 \overline{) 100} \\ \underline{100} \\ 0 \end{array}$$

$$\begin{array}{r} 1 \\ 5 \overline{) 100} \\ \underline{100} \\ 0 \end{array}$$

$$\begin{array}{r} 1 \quad 4 \quad 1 \\ 5 \overline{) 7205} \end{array}$$

$$\begin{array}{r} 1 \quad 5 \quad 3 \\ 4 \overline{) 6212} \end{array}$$



$612 \div 4 = 153$

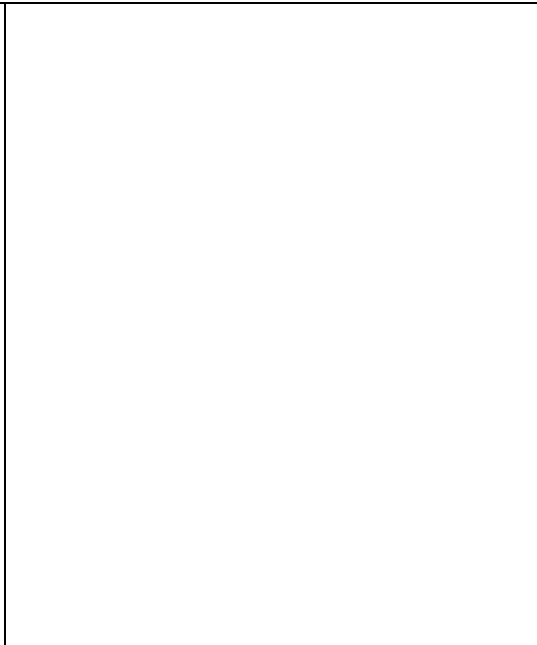
4  $\overline{) 612}$

1

4  $\overline{) 612}$

1

5



If there is a multiplicative change to the dividend factor and a corresponding change to the divisor, the quotient remains the same.



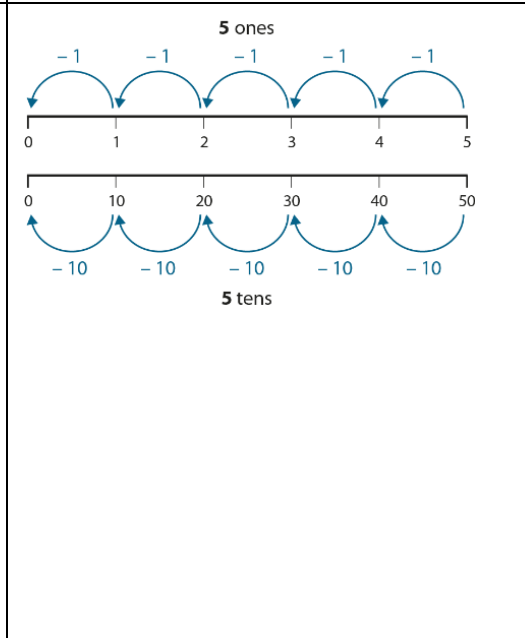
$$\begin{array}{c} 3 \\ \times 3 \\ \hline 9 \end{array} \div \begin{array}{c} 1 \\ \times 3 \\ \hline 3 \end{array} = 3$$

$$9 \div 3 = 3$$

If I multiply the dividend by \_\_, I must multiply the divisor by \_\_ for the quotient to remain the same.



**Year 5 and 6**

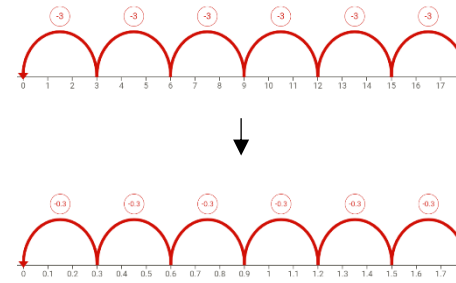
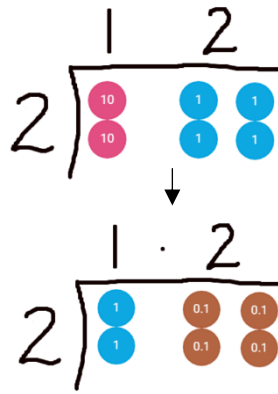


$$\begin{array}{c} 40 \\ \times 10 \\ \hline 400 \end{array} \div \begin{array}{c} 10 \\ \times 10 \\ \hline 100 \end{array} = 4$$

If the dividend is made one tenth of the size, the quotient will be one tenth of the size.

If the dividend is made one hundredth of the size, the quotient will be one hundredth of the size.

I move the digits of the dividend \_\_\_ places to the left until I get a whole number; then I divide; then I move the digits of the quotient \_\_\_ places to the right.



$$0.85 \div 5 = 0.17$$

$\times 100$  ↓  $85 \div 5 = 17$  ↗  $\div 100$

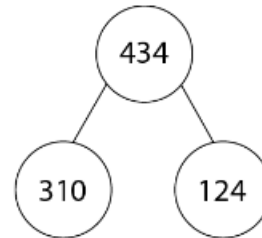
$$5 \overline{) 2255} \rightarrow 5 \overline{) 225.5}$$

### Year 5 onwards

Any two-, three- or four-digit dividend can be divided by a two-digit divisor using skip-counting in multiples of the divisor, or by short division or long division.

### Year 6

#### Partitioning



$$310 \div 31 = 10$$

$$124 \div 31 = 4$$

$$434 \div 31 = 14$$

#### Short division

$$\begin{array}{r} 0 \ 1 \ 4 \\ 31 \overline{) 4 \ 3 \ 2 \ 4} \end{array}$$

#### Long division

$$\begin{array}{r} 0 \ 1 \ 4 \\ 31 \overline{) 4 \ 3 \ 4} \\ \underline{3 \ 1} \phantom{0} \\ 1 \ 2 \ 4 \\ \underline{1 \ 2 \ 4} \\ 0 \end{array} \quad \begin{array}{l} (1 \text{ ten} \times 31 = 31 \text{ tens}) \\ (4 \text{ ones} \times 31 = 124 \text{ ones}) \end{array}$$

Where there is a remainder, the result can be expressed as a whole-number quotient with a whole-number remainder, a whole-number quotient with a proper-fraction remainder, or as a decimal-fraction quotient.

Year 6

$$354 \div 15 = ?$$

$$\begin{array}{r} 23 \text{ r}9 \\ 15 \overline{) 354} \\ \underline{30} \phantom{0} \\ 54 \\ \underline{45} \\ 9 \end{array}$$

So,  $354 \div 15 = 23 \text{ r}9$

$$\begin{array}{r} 23 \frac{9}{15} \\ 15 \overline{) 354} \\ \underline{30} \phantom{0} \\ 54 \\ \underline{45} \\ 9 \end{array}$$

$$\frac{9}{15} = \frac{3}{5}$$

So,  $354 \div 15 = 23 \frac{3}{5}$

$$\begin{array}{r} 23.6 \\ 15 \overline{) 354.0} \\ \underline{30} \phantom{0} \\ 54 \\ \underline{45} \\ 90 \\ \underline{90} \\ 0 \end{array}$$

So,  $354 \div 15 = 23.6$

This policy should be reviewed every two years, or as necessary.

Log of changes and updates to the document:

Date	Page	Change	Approver
5/11/2020	All	Policy created by Maths Leader – EM and reviewed with HT	KL
11/11/2020	All	Reviewed at staff meeting	
	All	Reviewed by governors	SDC
10/12/2021	All	None	KL SDC
February 2023	1	Update logo and dates	KL and EH
	All	Update and add to policy, reflecting the current practise, with specific examples in Year groups  Update to HT, Maths SL and Link Governor	MH

